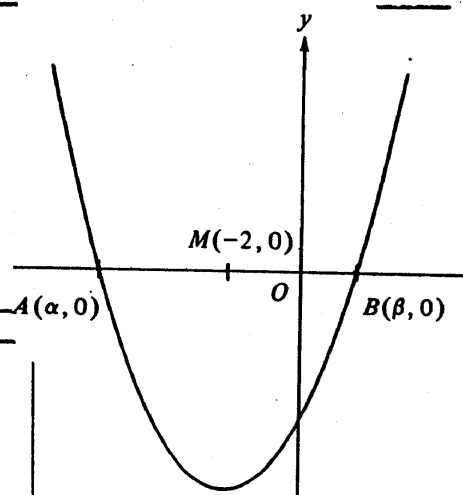
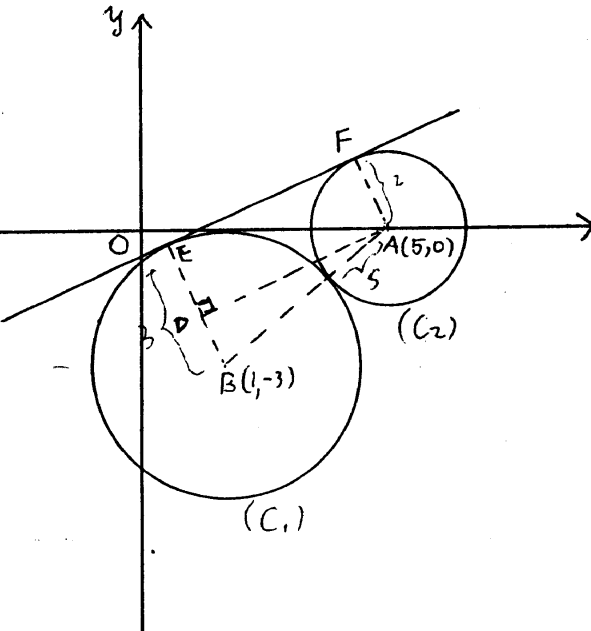


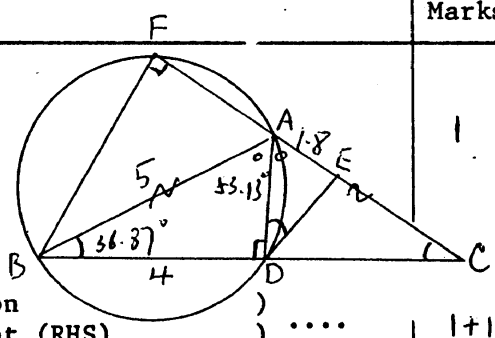
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Solutions	Marks	Remarks
<p>6. (a) α and β are the roots of $x^2 + px + q = 0$.</p> <p>$\therefore \alpha + \beta = -p$</p> <p>$M(-2, 0)$ is the mid-point of AB</p> <p>$\therefore \frac{\alpha + \beta}{2} = -2$</p> <p>$p = 4$</p> <p>(b) Now $\alpha\beta = q$</p> <p>$(\alpha + \beta)^2 = \alpha^2 + \beta^2 + 2\alpha\beta$</p> <p>$(-4)^2 = 26 + 2q$</p> <p>$\therefore q = \frac{16 - 26}{2}$</p> <p>$= -5$</p>	<p>1A</p> <p>1A</p> <p>$\frac{1A}{3}$</p> <p>1A</p> <p>1M</p> <p>$\frac{1A}{3}$</p>	 <p>Formula correct</p>
<p>7. (a) The remainder is $(-1)^{1000} + 6$</p> <p>$= 7$</p> <p>(b) (i) Putting $x = 8$,</p> <p>by (a), the remainder is 7</p> <p>(ii) The remainder of 8^{1000} when divided by 9 is $7 - 6$</p> <p>$= 1$</p>	<p>1M</p> <p>$\frac{1A}{2}$</p> <p>1M</p> <p>1A</p> <p>1M</p> <p>$\frac{1A}{6}$</p>	<p>Optional</p> <p>optional, or quoting result in (a)</p> <p>optional</p>

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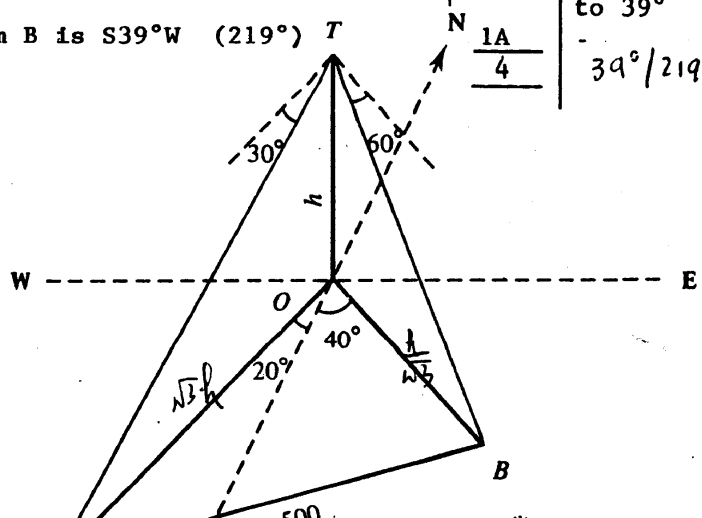
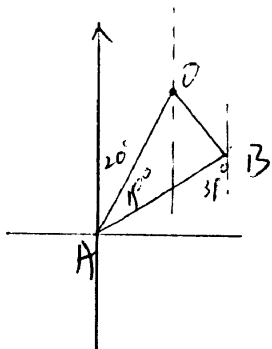
Solutions	Marks	Remarks
<p>8. (a) Centre = (1, -3)</p> <p>Radius = $\sqrt{(-1)^2 + (3)^2} - 1 = 3$</p>	1A	$x=1, y=-3$
	<u>1A</u>	
	<u>2</u>	
<p>(b) Distance between the centre and A</p> <p style="margin-left: 20px;">$= \sqrt{(5-1)^2 + (0-(-3))^2}$</p> <p style="margin-left: 20px;">$= 5$</p> <p style="margin-left: 20px;">> radius of (C_1) (=3))</p> <p style="margin-left: 20px;">∴ A lies outside (C_1))...)</p>	1M	
	1A	
	1M	
	<u>3</u>	
<p>(c) (i) $s = 5 - 3$</p> <p style="margin-left: 40px;">$= 2$</p>	1M	
	1A	
	<u>2</u>	
<p>(ii) Equation of (C_2) is $(x-5)^2 + (y-0)^2 = 2^2$</p> <p style="margin-left: 40px;">or $x^2 + y^2 - 10x + 21 = 0$</p>	1A	
	<u>3</u>	
<p>(d)</p> 	1	<p>For sketch. A line touching two circles at 2 distinct points. May draw the other common tangent. Follow through.</p>
	$EF = DA$) $BD = BE - AF$) $EF = \sqrt{AB^2 - BD^2}$ $= \sqrt{5^2 - (3-2)^2}$ 1M+1A $= \sqrt{24}$ 1A $= 2\sqrt{6} (= 4.90)$	<p>Any figure roundable to 4.90</p>
	<u>4</u>	

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Solutions	Marks	Remarks
<p>9.(a) Consider Δs ABD and ACD. As AB is a diameter, $\angle ADB = 90^\circ$.</p> <p>As BDC is a straight line, $\angle ADC = 90^\circ$</p> <p>As AB = AC and AD is common Δ ABD and Δ ACD are congruent (RHS)</p>		<p style="text-align: center;">1</p> <p style="text-align: center;">1 for AD=AD / AB=AC / $\angle ABD = \angle ACD$. 1 for correct reasoning</p>
<p>(b) Consider Δs ABD and ADE $\therefore \Delta ABD \cong \Delta ADE$ $\angle BAD = \angle CAD$</p> <p>Since DE is a tangent, $\angle ADE = \angle ABD$ (\angle in alt. seg.) $\therefore \Delta ABD \sim \Delta ADE$</p>	<p>1</p> <p>1</p> <hr style="width: 50%; margin: 0 auto;"/> <p style="text-align: center;">2</p>	
<p>(c) (i) As $\angle ADB = 90^\circ$ $AD = \sqrt{AB^2 - BD^2}$ $= \sqrt{5^2 - 4^2} = 3$</p> <p>$\therefore \Delta ABD \sim \Delta ADE$ $\frac{DE}{3} = \frac{4}{5}$ $\frac{AB}{AD} = \frac{BD}{DE}, \frac{5}{3} = \frac{4}{DE}$</p> <p>$\therefore DE = 2 \frac{2}{5} (= 2.4)$</p>	<p>1A</p> <p>1M</p> <p>1A</p>	<p><u>OR</u></p> <p>AD = 3 1A</p> <p>$\angle ABD = \cos^{-1} 0.8$ 1M</p> <p>DE = $3 \cos 36.87^\circ$ = 2.4 1A</p>
<p>(ii) Consider Δs BCF and ABD \therefore AB is a diameter, $\angle AFB = 90^\circ$ $= \angle ADB$</p> <p>As $\angle BCF = \angle ABD$, Δs BCF and ABD are similar</p> <p>$\frac{AF + 5}{8} = \frac{4}{5}$ $AF = 1 \frac{2}{5} (= 1.4)$</p>	<p>1</p> <p>1</p> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p style="text-align: center;">1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p style="text-align: center;">7</p>	
<p><u>Alternatively</u></p>		
<p>(a) \therefore AB is a diameter, $\angle ADB = 90^\circ$ \therefore ABC is an isosceles triangle and $BC \perp AD$</p> <p>$\Delta ABD \cong \Delta ACD$</p>	<p>1A</p> <p>1</p> <p>1</p>	<p>May also use AAS</p>
<p>(c)(ii) (1) $\angle ACB = \angle ABC = 36.87^\circ$ $\angle AFB = 90^\circ$ $\frac{AF + 5}{8} = \cos 36.9^\circ$ $AF = 1.40$</p>	<p>1A</p> <p>1</p> <p>1A</p> <p>1A</p>	<p>Accept 36.9° optional</p>
<p>(2) $\angle ABC = \angle ACB = 36.87^\circ$ $\angle AFB = 90^\circ$ $\angle BAF = \angle ABC + \angle ACB = 73.7^\circ$ $\cos 73.7^\circ = \frac{AF}{5}$ $AF = 1.40$</p>	<p>1A</p> <p>1</p> <p>1A</p>	<p>Accept 36.9° optional</p>

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Solutions	Marks	Remarks
<p>10.(a) $\frac{OT}{OA} = \tan 30^\circ$ ($\frac{CA}{CT} = \tan 60^\circ$)</p> <p>$\therefore OA = \frac{h}{\tan 30^\circ}$</p> <p style="padding-left: 40px;">$= h\sqrt{3}$ metres ($= 1.73h$)</p> <p>Similarly $OB = \frac{h}{\tan 60^\circ} = \frac{h}{\sqrt{3}}$ metres ($= 0.577h$)</p>	<p>1A</p> <p>1A</p> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>3</p>	<p>2 + 1</p>
<p>(b) $\angle AOB = 60^\circ$</p> <p>By the cosine rule,</p> <p>$AB^2 = OA^2 + OB^2 - 2(OA)(OB)\cos \angle AOB$</p> <p style="padding-left: 40px;">$= (h\sqrt{3})^2 + (\frac{h}{\sqrt{3}})^2 - 2(h\sqrt{3})(\frac{h}{\sqrt{3}})\cos 60^\circ$</p> <p style="padding-left: 40px;">$= 3h^2 + \frac{h^2}{3} - h^2$</p> <p style="padding-left: 40px;">$= \frac{7}{3}h^2$</p> <p>$\therefore AB = h\sqrt{\frac{7}{3}}$ metres (1.53h)</p> <p>As $h\sqrt{\frac{7}{3}} = 500$</p> <p style="padding-left: 40px;">$h = 500\sqrt{\frac{3}{7}}$ ($= 327$ or 328)</p>	<p>1A</p> <p>1M</p> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>5</p>	<p>Any fig. roundable to 1.53h</p> <p>Any figure roundable to 327 or 328</p>
<p>(c) By the sine rule $\frac{R/\sqrt{3}}{\sin \angle OAB} = \frac{500}{\sin 60^\circ}$</p> <p>$\sin \angle OAB = \frac{h}{\sqrt{3}} \times \frac{\sin 60^\circ}{500}$</p> <p style="padding-left: 40px;">$= \frac{500\sqrt{\frac{3}{7}}}{\sqrt{3}} \times \frac{\sqrt{3}}{500} = \frac{1}{2}\sqrt{\frac{3}{7}}$ (0.327)</p> <p>$\therefore \angle OAB = 19.1^\circ = 19^\circ$ (correct to the nearest degree)</p>	<p>1M</p> <p>1A</p>	
<p>(i) The bearing of B from A is N39°E (039° or 39°)</p> <p>(ii) The bearing of A from B is S39°W (219°)</p>	<p>1A</p> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>4</p>	<p>Accept figure roundable to 39°</p> <p>39°/219°</p>

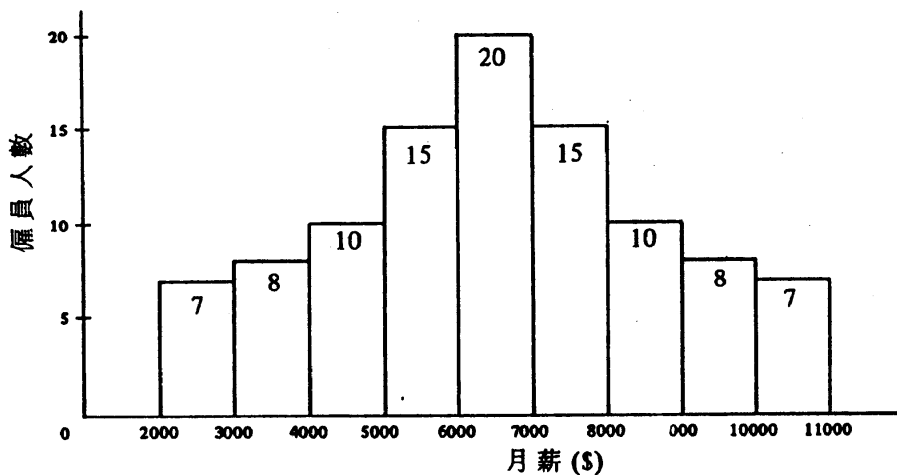


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Solutions	Marks	Remarks																		
<p>11.(a) (i) $S = 2\pi r^2 + 2\pi rh$</p> <p>(ii) As $V = \pi r^2 h$, $h = \frac{V}{\pi r^2}$</p> $S = 2\pi r^2 + 2\pi r \left(\frac{V}{\pi r^2} \right)$ $= 2\pi r^2 + \frac{2V}{r}$	<p>1A</p> <p>1M</p> <hr style="width: 50%; margin: 0 auto;"/> <p>1</p> <hr style="width: 50%; margin: 0 auto;"/> <p>3</p>	<p>OR</p> $2\pi r^2 + \frac{2V}{r} = 2\pi r^2 + \frac{2(\pi r^2 h)}{r}$ $= S$																		
<p>(b) Putting $V = 2\pi$, $S = 6\pi$</p> $6\pi = 2\pi r^2 + \frac{2(2\pi)}{r}$ $\therefore r^3 - 3r + 2 = 0$ <p>By inspection, $r = 1$ is a root (or $r = -2$)</p> $\therefore r^3 - 3r + 2 = (r - 1)(r^2 + r - 2)$ $= (r - 1)^2(r + 2)$ $= 0$ <p>i.e. $r = 1$ (as $r \neq -2$)</p>	<p>1.</p> <p>1A</p> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>4</p>	<p>OR $r-1$ is a factor</p> <p>OR $r+2$ is a factor</p>																		
<p>(c) Putting $V = 3\pi$, $S = 10\pi$, we have</p> $10\pi = 2\pi r^2 + \frac{2(3\pi)}{r}$ $r^3 - 5r + 3 = 0$ <p>Let $f(r) = r^3 - 5r + 3$</p> <p>$f(1) < 0$ and $f(2) > 0$, there is a root of $f(r) = 0$ between 1 and 2</p>	<p>1A</p> <p>1A</p>	<p>Signs of $f(1)$, $f(2)$</p>																		
<table border="1" style="width: 100%; border-collapse: collapse; margin-bottom: 10px;"> <thead> <tr> <th style="width: 30%;">Interval</th> <th style="width: 30%;">Mid -value, r_1</th> <th style="width: 20%;">f(r_1)</th> </tr> </thead> <tbody> <tr> <td>$1 < r < 2$</td> <td>1.5</td> <td>-</td> </tr> <tr> <td>$1.5 < r < 2$</td> <td>1.75</td> <td>-</td> </tr> <tr> <td>$1.75 < r < 2$</td> <td>1.875</td> <td>+</td> </tr> <tr> <td>$1.75 < r < 1.875$</td> <td>1.8125 (1.813)</td> <td>-</td> </tr> <tr> <td>$1.8125 < r < 1.875$</td> <td>1.84375 (1.844)</td> <td>+</td> </tr> </tbody> </table> <p>$\therefore 1.8125 < r < 1.84375$</p> <p>$\therefore r = 1.8$ (correct to 1 d.p.)</p>	Interval	Mid -value, r_1	f(r_1)	$1 < r < 2$	1.5	-	$1.5 < r < 2$	1.75	-	$1.75 < r < 2$	1.875	+	$1.75 < r < 1.875$	1.8125 (1.813)	-	$1.8125 < r < 1.875$	1.84375 (1.844)	+	<p>1M</p> <p>1M</p> <hr style="width: 50%; margin: 0 auto;"/> <p>1A</p> <hr style="width: 50%; margin: 0 auto;"/> <p>5</p>	<p>Testing ^{sign} at mid-value</p> <p>Choosing interval</p>
Interval	Mid -value, r_1	f(r_1)																		
$1 < r < 2$	1.5	-																		
$1.5 < r < 2$	1.75	-																		
$1.75 < r < 2$	1.875	+																		
$1.75 < r < 1.875$	1.8125 (1.813)	-																		
$1.8125 < r < 1.875$	1.84375 (1.844)	+																		

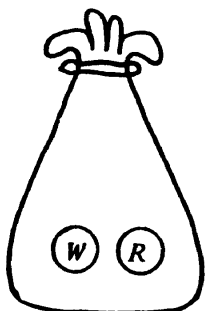
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Solutions	Marks	Remarks
<p>12.(a) (i) The modal class is \$6000 - \$7000</p> <p>By symmetry of the distribution, the median salary = \$6500, the mean salary = \$6500.</p> <p>The interquartile range = 8000 - 5000 = \$3000</p> <p>The mean deviation</p> $= \frac{1}{100} \times 2 [7(6500 - 2500) + 8(6500 - 3500) + 10(6500 - 4500) + 15(6500 - 5500)]$ <p>= \$1740</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p><u>1A</u></p> <p><u>7</u></p>	<p>Accept \$6500</p> <p><i>Optional</i></p>
<p>(ii) The standard deviation of salaries will become smaller because the salaries of the additional 10 employees have no deviation from the mean while the total number of employees has become larger.</p>	<p>1A</p> <p>1</p> <p><u>2</u></p>	<p>For answer</p> <p><u>OR</u> By calculation</p> <p>$\sum (x - \bar{x})^2$ unchanged $\sum f$ is greater</p>
<p>(b) The standard deviation</p> $= \sqrt{\frac{1}{7} (9 + 4 + 1 + 0 + 1 + 4 + 9)}$ <p>= 2</p>	<p>2A</p> <p><u>1A</u></p> <p><u>3</u></p>	

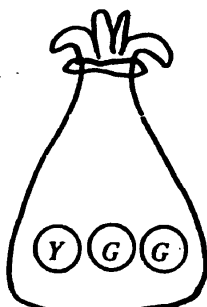


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Solutions	Marks	Remarks
<p>13.(a) (i) The probability that Bag B is chosen = $\frac{1}{3}$.</p> <p>\therefore the probability that the ball drawn is green</p> $= \frac{1}{3} \times \frac{2}{3}$ $= \frac{2}{9} \quad (0.222)$	1A	
<p>(ii) the probability that Bag B is chosen and the yellow ball is drawn = $\frac{1}{3} \times \frac{1}{3}$</p> $= \frac{1}{9} \quad (0.111)$ <p>\therefore the required probability = $\frac{1}{3} \times \frac{1}{3} + \frac{1}{3} \times 1$</p> $= \frac{4}{9} \quad (0.444)$	1M 1A	$P_1 \times P_2$
	1A	OR probability of drawing \textcircled{Y} from bag C.
	1M	$P_1 + P_2$ $\frac{1}{3} \times \frac{1}{3} \times 1$ no mark
	<u>1A</u>	
	<u>6</u>	
<p>(b) (i) The probability that Peter and Alice both draw a green ball = $\frac{2}{9} \times \frac{2}{9}$</p> $= \frac{4}{81} \quad (0.0494)$	1M	Followed from (a)(i)
	1A	
<p>(ii) The probability that they both draw a yellow ball from Bag B = $\frac{1}{9} \times \frac{1}{9}$</p> $= \frac{1}{81} \quad (0.0123)$ <p>The probability that they both draw a yellow ball from Bag C = $\frac{1}{3} \times \frac{1}{3}$</p> $= \frac{1}{9} \quad (0.111)$ <p>\therefore the required probability = $\frac{1}{81} + \frac{1}{9}$</p> $= \frac{10}{81} \quad (0.123)$	1A	
	1A	
	<u>1A</u>	
	<u>2A</u>	
	<u>6</u>	



A 袋



B 袋



C 袋

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Solutions	Marks	Remarks
14.(a) (i) The integers in G_6 are 16, 17, 18, 19, 20, 21	1M+1A	1M for 6 consecutive integers (5 correct)
(ii) The total number of integers in G_1, G_2, \dots, G_6 $= 1 + 2 + 3 + \dots + 6$ $= 21$	1A <hr style="width: 50%; margin: auto;"/> 1A	Optional
(b) (i) $u_{k-1} = 1 + 2 + \dots + (k-1)$ $= \frac{(k-1)}{2} [1 + (k-1)]$ $= \frac{k(k-1)}{2}$	1A 1M 1A	Sum of AP = $\frac{n}{2}[a + l]$
\therefore The first term in $G_k = \frac{k(k-1)}{2} + 1 (= \frac{k^2-k+2}{2})$	1M+1A	1M for $v_1 = u_{k-1} + 1$
(ii) The sum of all integers in G_k $= \frac{k}{2} [2 (\frac{k(k-1)}{2} + 1) + (k-1) \times 1]$ $= \frac{k(k^2+1)}{2} (= \frac{k^3+k}{2})$	1M+1A <hr style="width: 50%; margin: auto;"/> 1A	1M for Sum of AP