

HKCEE 1982 Mathematics II

82
1. $\frac{2a}{a^2 - 4b^2} + \frac{1}{2b - a} =$

- A. $\frac{1}{a + 2b}$
 B. $\frac{2a - 1}{(a + 2b)(a - 2b)}$
 C. $\frac{2a + 1}{(a + 2b)(a - 2b)}$
 D. $\frac{3a + 2b}{(a + 2b)(a - 2b)}$
 E. $\frac{a + 2b}{(a + 2b)(a - 2b)}$

82
2. $\frac{8^{2x} \cdot 4^{3x}}{2^x \cdot 16^{2x}} =$

- A. 2^{3x}
 B. 2^{2x}
 C. 2^x
 D. 8
 E. 1

82
3. $(a^{-2} - 3b^{-1})^{-1} =$

- A. $\frac{3a^2 + b}{a^2b}$
 B. $\frac{3a^2 - b}{a^2b}$
 C. $\frac{3b - a^2}{a^2b}$
 D. $\frac{3a^2b}{b - 3a^2}$
 E. $\frac{3a^2b}{3b - a^2}$

82
4. If $x = \frac{1}{\frac{1}{y} + \frac{2}{z}}$, then $y =$

- A. $\frac{2x}{z}$
 B. $\frac{z}{xz - z}$
 C. $\frac{z - 2x}{xz}$
 D. $\frac{xz}{2x + z}$
 E. $\frac{xz}{z - 2x}$

82
5. If $10^{kx+a} = P$, then $x =$

- A. $\frac{1}{k}(10^{P-a})$
 B. $\log_{10} \frac{P-a}{k}$
 C. $\frac{1}{k} \log_{10} P - a$
 D. $\frac{1}{k} (\log_{10} P - a)$
 E. $\frac{1}{k} (\log_{10} P + a)$

82
6. α and β are the roots of the equation $x^2 - 5x - 7 = 0$. What is the equation whose roots are $\alpha + 1$ and $\beta + 1$?

- A. $x^2 - 3x + 3 = 0$
 B. $x^2 - 3x - 11 = 0$
 C. $x^2 - 5x + 1 = 0$
 D. $x^2 - 7x - 1 = 0$
 E. $x^2 - 7x - 7 = 0$

82
7. What are the roots of the equation $(x - 3)^2(x + 1) = -(x + 1)^2(x - 3)$?

- A. 1 only
 B. 1, -3 only
 C. -1, 3 only

D. $1, -1, -3$

E. $1, -1, 3$

82 8. $5 - 9x - 2x^2 > 0$ is equivalent to

A. $x > \frac{1}{2}$

B. $x < -5$

C. $-5 < x < \frac{1}{2}$

D. $x < -5$ or $x > \frac{1}{2}$

E. $x > -5$ or $x < \frac{1}{2}$

82 9. What will \$P amount to in 3 years' time. If interest is compounded monthly at 12% per annum?

A. $\$P(1 + \frac{36}{100})$

B. $\$P(1 + \frac{1}{100})^{36}$

C. $\$P(1 + \frac{12}{100})^{36}$

D. $\$P(1 + \frac{12}{100})^3$

E. $\$P(1 + \frac{1}{100})^3$

82 10. A child spent $\frac{1}{10}$ of his saving on a shirt and $\frac{1}{5}$ of his savings on a pair of trousers. He then spent 30% of the rest of his savings on books. What percentage of his saving did he spend altogether?

A. 49.6%

B. 50.4%

C. 51%

D. 58%

E. 60%

82 11. The rent of a flat is raised by 30% every two years beginning from a fixed date. Counting from that date, after how many years will the rent just exceed twice the original rent?

A. 4 years

B. 5 years

C. 6 years

D. 7 years

E. Over 7 years

82 12. A man drives 20 km at 40km/h. At what speed must he drive on his return journey so that the average speed for the double journey is 60 km/h?

A. 50 km/h

B. 80 km/h

C. 100 km/h

D. 120 km/h

E. 160 km/h

82 13. The marked price of a book is \$240. If the book is sold at a discount of 20%, the profit will be 20% of the cost price. What is the cost price of the book?

A. \$153.6

B. \$160

C. \$192

D. \$200

E. \$240

82 14. A right circular cone of altitude $3r$ and base radius r has the same volume as a cube of side x . $x =$

A. πr^3

B. πr

C. $\frac{1}{3} \pi r$

D. $\sqrt[3]{3\pi} r$

E. $\sqrt[3]{\pi} r$

82 Some air escapes from a spherical balloon of volume a^3 . The balloon keeps its spherical shape and is now of volume b^3 . What is the percentage decrease in the radius?

- A. $\frac{a-b}{a} \times 100\%$
 B. $\frac{a-b}{b} \times 100\%$
 C. $\sqrt[3]{\frac{a^3-b^3}{a^3}} \times 100\%$
 D. $\sqrt[3]{\frac{a^3-b^3}{b^3}} \times 100\%$
 E. $\frac{a^3-b^3}{a^3} \times 100\%$

82 Coffee A and coffee B are mixed in the ratio 1 : 2. A profit of 20% on the cost price is made by selling the mixture at \$36/kg. If the cost price of A is \$12/kg, what is the cost price of B?

- A. \$18/kg
 B. \$24/kg
 C. \$39/kg
 D. \$48/kg
 E. \$66/kg

82 $(\sin \theta + \cos \theta)^2 - 1 =$
 17.

- A. 0
 B. 1
 C. $2 \cos^2 \theta$
 D. $2 \sin \theta \cos \theta$
 E. $-2 \sin \theta \cos \theta$

82 If $\tan x = -\frac{3}{4}$ and x is an angle in the second quadrant, what is the value of $\sin x + \cos x$?

- A. $-\frac{7}{5}$

- B. $-\frac{1}{5}$
 C. $\frac{1}{5}$
 D. 1
 E. $\frac{7}{5}$

82 If $A + B = 180^\circ$, which of the following is/are true?

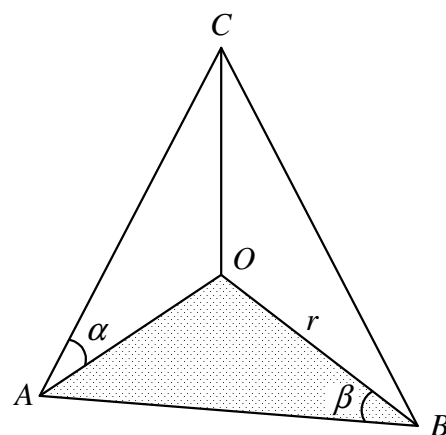
- I. $\sin A = \sin B$
 II. $\cos A = \cos B$
 III. $\tan A = \tan B$

- A. I only
 B. II only
 C. III only
 D. I, II and III
 E. None of them

82 From the top of a lighthouse, h metres high, the angle of depression of a boat is 20° . How far is the boat from the base of the lighthouse, which is at sea-level?

- A. $h \sin 20^\circ$ m
 B. $h \cos 20^\circ$ m
 C. $h \tan 20^\circ$ m
 D. $\frac{h}{\sin 20^\circ}$ m
 E. $\frac{h}{\tan 20^\circ}$ m

82
 21.



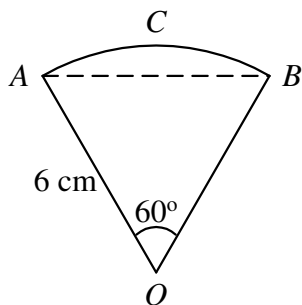
In the figure, OAB is a right-angled triangle in a horizontal plane with $\angle AOB = 90^\circ$. OC is a vertical line. If $OB = r$, $AC =$

- A. $\frac{r \sin \beta}{\tan \alpha}$
- B. $\frac{r \tan \alpha}{\cos \beta}$
- C. $\frac{r \sin \beta}{\sin \alpha}$
- D. $\frac{r \cos \beta}{\tan \alpha}$
- E. $\frac{r \tan \beta}{\cos \alpha}$

82 In a circle, the angle of a sector is 30°
22. and the radius is 2 cm. The area of the sector is

- A. 120 cm^2
- B. 60 cm^2
- C. $\frac{30}{\pi} \text{ cm}^2$
- D. $\frac{2\pi}{3} \text{ cm}^2$
- E. $\frac{\pi}{3} \text{ cm}^2$

82
23.

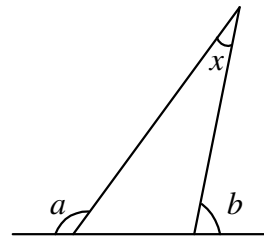


In the figure, $OACB$ is a sector of a circle of radius 6 cm. Arc ACB is longer than the chord AB by

- A. $(\pi - 3) \text{ cm}$
- B. $2(\pi - 3) \text{ cm}$
- C. $3(\pi - 1) \text{ cm}$
- D. $6(\pi - 1) \text{ cm}$

E. $3(2\pi - \sqrt{3}) \text{ cm}$

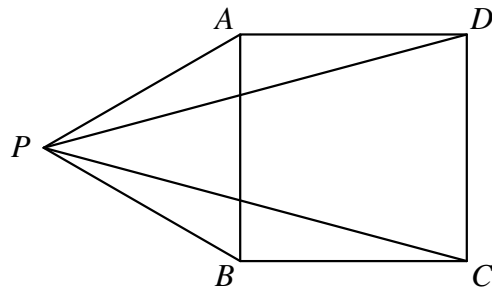
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24.



In the figure, $x =$

- A. $a - b$
- B. $a + b - 180^\circ$
- C. $a + b - 90^\circ$
- D. $180^\circ - a + b$
- E. $360^\circ - a - b$

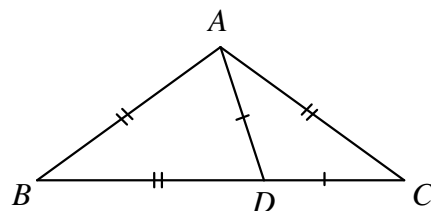
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25.



In the figure, $ABCD$ is a square and PAB is an equilateral triangle. $\angle CPD =$

- A. 20°
- B. 25°
- C. 30°
- D. 32°
- E. 36°

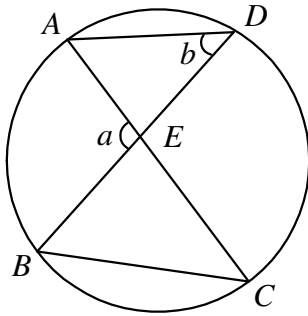
82
26.



In the figure, D is a point on BC such that $AD = CD$ and $AB = AC = BD$. $\angle B =$

- A. $22\frac{1}{2}^\circ$
- B. 30°
- C. 36°
- D. 45°
- E. 60°

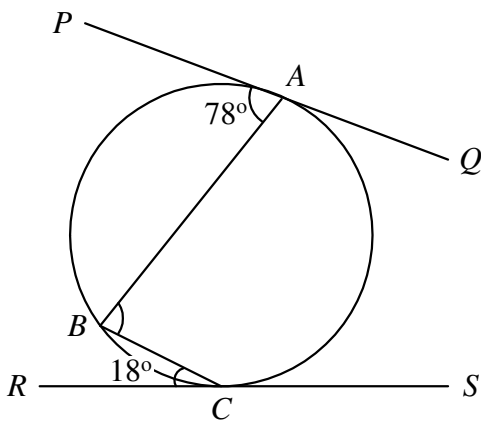
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27.



In the figure, AKC and BKD are two chords of the circle. $\angle CBD =$

- A. $a - b$
- B. $a + b$
- C. $a + b - 90^\circ$
- D. $\frac{1}{2}a$
- E. $\frac{1}{2}a + b$

82
28.



In the figure, PQ and RS touch the circle at A and C respectively. $\angle ABC =$

- A. 48°
- B. 60°
- C. 84°
- D. 90°
- E. 96°

82 If $f(x) = 5x + 1$, then $f(x + 1) - f(x) =$

- A. 1
- B. 6
- C. $4 \cdot 5^x$
- D. $5 \cdot 5^x$
- E. $4 \cdot 5^x + 1$

82
30. $\log_{10}(x^{\log_{10} x}) =$

- A. $(\log_{10} x)^2$
- B. $\log_{10}(x^2)$
- C. $x \log_{10} x$
- D. $\log_{10}(\log_{10} x)$
- E. 10^{x^2}

82
31. The graphs of $y = \frac{x^2}{2}$ and $y = x + 2$

intersect at the points (x_1, y_1) and (x_2, y_2) . Which of the following equations has roots x_1 and x_2 ?

- A. $x^2 - x - 2 = 0$
- B. $x^2 + x + 2 = 0$
- C. $x^2 - 2x - 4 = 0$
- D. $x^2 - 4x - 8 = 0$
- E. $2x^2 - x - 2 = 0$

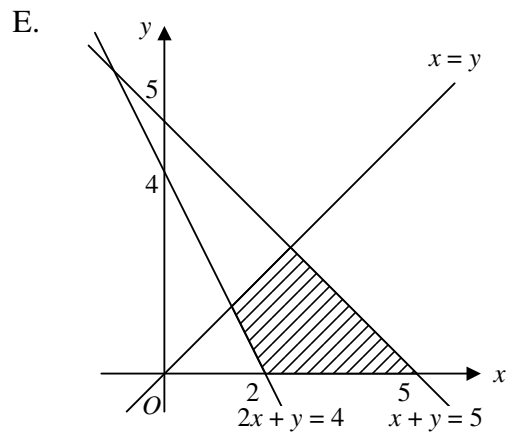
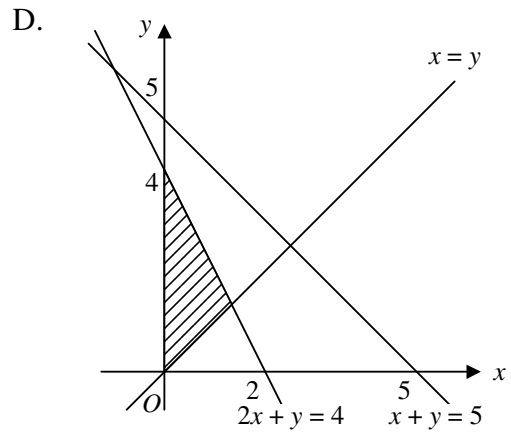
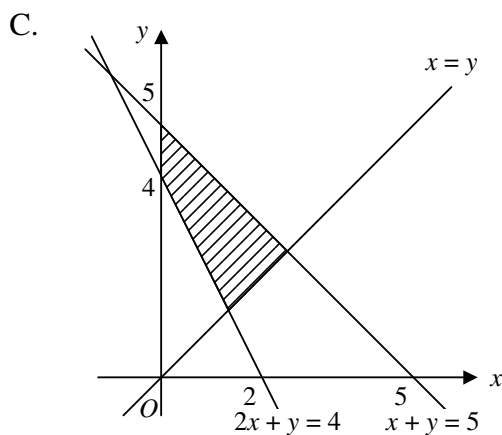
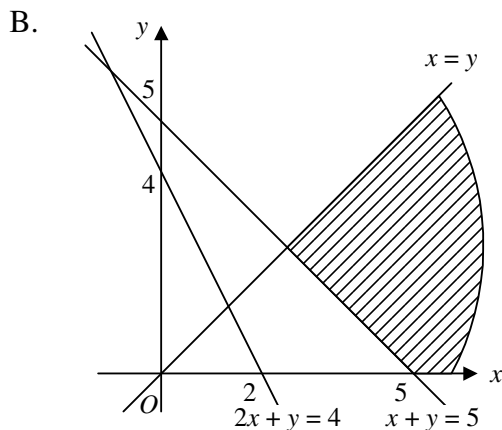
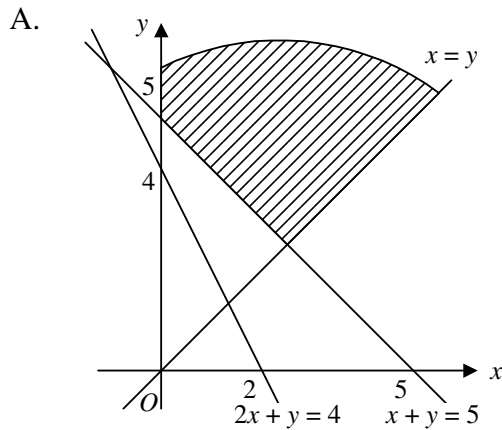
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32. Let $a > 2$. The inequality $2x - 2a < ax + 5a$ is equivalent to

- A. $x > \frac{7a}{2-a}$
- B. $x < \frac{7a}{2-a}$
- C. $x > \frac{-3a}{2-a}$
- D. $x < \frac{-3a}{2-a}$
- E. $x > \frac{-7a}{2-a}$

82
33.

$$\text{If } \begin{cases} x \geq 0, \\ y \geq 0, \\ x + y \leq 5, \\ 2x + y \geq 4, \\ x \geq y, \end{cases}$$

in which of the following shaded regions do all the points satisfy the above inequalities?



82 a , b and k are real numbers. If $k > 0$
34. and $a > b$, which of the following must be true?

- I. $a^2 > b^2$
- II. $-a < -b$
- III. $ka > kb$

- A. II only
- B. III only
- C. I and III only
- D. II and III only
- E. I, II and III

82 \$9000 is divided among A , B and C .
35. A 's share, B 's share and C 's share, in that order, form an arithmetic progression. If B 's share is three times A 's share, how much does C get?

- A. \$1500
- B. \$3000
- C. \$4500
- D. \$5000
- E. \$6000

82 1, -0.1, 0.01, -0.001, ... is a geometric progression. What is its sum to infinity?

- A. 0
- B. 1
- C. 0.99
- D. $\frac{10}{11}$
- E. $\frac{10}{9}$

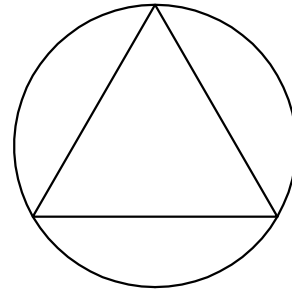
82 If $x \neq 0$, which of the following is/are geometric progression?

- I. x, x^2, x^3, x^4
 - II. $x, 2x, 3x, 4x$,
 - III. $x, -x^2, x^3, -x^4$
- A. I only
 - B. I and II only
 - C. I and III only
 - D. II and III only
 - E. I, II and III

82 The average of x and y is a , the average of y and z is b , and the average of x and z is c . What is the average of x, y and z ?

- A. $\frac{1}{6}(a + b + c)$
- B. $\frac{1}{3}(a + b + c)$
- C. $\frac{1}{2}(a + b + c)$
- D. $\frac{2}{3}(a + b + c)$
- E. $\frac{3}{2}(a + b + c)$

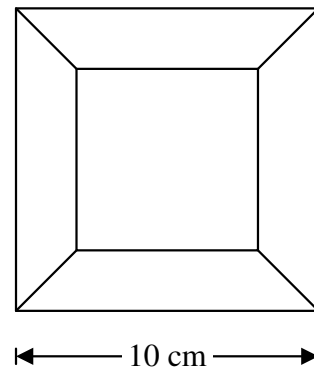
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39.



In the figure an equilateral triangle is inscribed in a circle of radius a . What is the area of the triangle?

- A. $\frac{3}{2}a^2$
- B. $\frac{3\sqrt{3}}{4}a^2$
- C. $\frac{3}{4}a^2$
- D. a^2
- E. $\frac{3\sqrt{3}}{2}a^2$

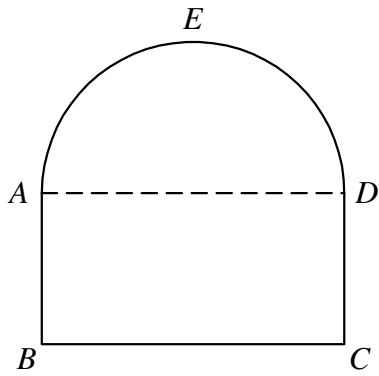
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40.



Four identical trapeziums, each of area 16 cm^2 , are drawn inside a square of side 10 cm as shown in the figure. What is the height of each trapezium?

- A. $\frac{1}{2} \text{ cm}$
- B. 1 cm
- C. 2 cm
- D. 3 cm
- E. 4 cm

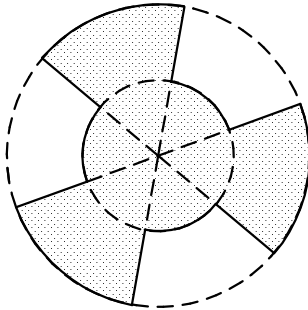
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41.



The perimeter of the given figure $ABCDE$ is $2(\pi + 4)$ cm. The upper portion AED is a semi-circle and the lower portion $ABCD$ is a rectangle. $AB : BC = 1 : 2$. What is the area of the given figure?

- A. 8 cm^2
- B. $2\pi \text{ cm}^2$
- C. $4\pi \text{ cm}^2$
- D. $4(\pi + 2) \text{ cm}^2$
- E. $2(\pi + 4) \text{ cm}^2$

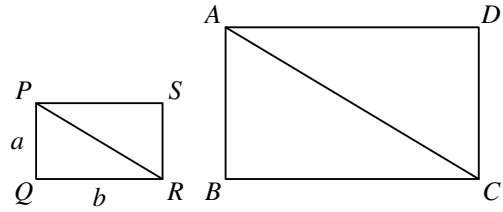
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42.



In the figure, the two concentric circles are of radius 2 cm and 4 cm respectively. Each circle is divided into 6 equal parts by 6 radii. What is the area of the shaded region?

- A. $12\pi \text{ cm}^2$
- B. $10\pi \text{ cm}^2$
- C. $9\pi \text{ cm}^2$
- D. $6\pi \text{ cm}^2$
- E. $2\pi \text{ cm}^2$

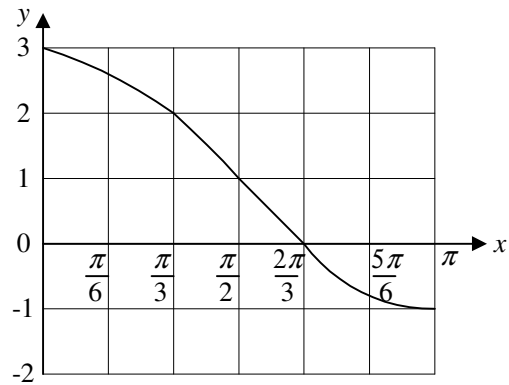
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43.



In the figure, the rectangles are similar. $PQ = a$, $QR = b$. If $AC = 2PR$, what is the area of $ABCD$?

- A. $2ab$
- B. $4ab$
- C. $2(a^2 + b^2)$
- D. $2(a + b)\sqrt{a^2 + b^2}$
- E. $2ab\sqrt{a^2 + b^2}$

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44.



The above figure shows the graph of $y = a \cos x + 1$ for $0 \leq x \leq \pi$. $a =$

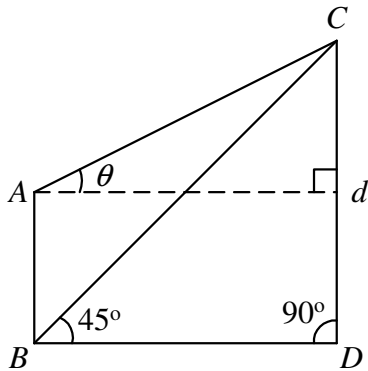
- A. -1
- B. 0
- C. 1
- D. 2
- E. 3

82
45.
$$\frac{\sin \theta + \cos \theta}{\sin \theta - \cos \theta} + \frac{\sin \theta - \cos \theta}{\sin \theta + \cos \theta} =$$

- A. 2
- B. $4 \sin \theta \cos \theta$
- C. $\frac{2 \sin \theta \cos \theta}{\sin^2 \theta - \cos^2 \theta}$
- D. $\frac{4 \sin \theta \cos \theta}{\sin^2 \theta - \cos^2 \theta}$

E. $\frac{2}{\sin^2 \theta - \cos^2 \theta}$

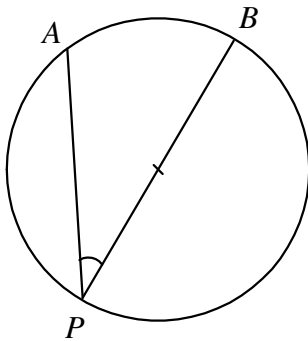
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46.



AB and CD are two buildings of heights h and d respectively. The angles of elevation of C from A and B are respectively θ and 45° . $d =$

- A. $h(1 - \tan \theta)$
- B. $h(1 + \tan \theta)$
- C. $h \tan \theta$
- D. $\frac{h}{1 + \tan \theta}$
- E. $\frac{h}{1 - \tan \theta}$

82
47.



In the figure, BP is a diameter of the circle. The minor arc AB and the radius are of equal length. $\angle APB =$

- A. $\frac{1}{2}$ rad
- B. 1 rad
- C. $\frac{\pi}{6}$ rad

D. $\frac{\pi}{4}$ rad

E. $\frac{\pi}{3}$ rad

82 How many roots has the equation

48. $\sin \theta + \sin^2 \theta = \cos^2 \theta$
where $0^\circ \leq \theta \leq 360^\circ$?

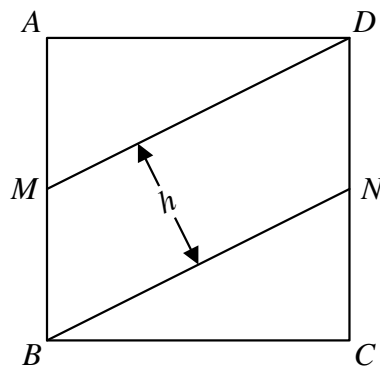
- A. 0
- B. 1
- C. 2
- D. 3
- E. 4

82 If $0 \leq x \leq \pi$ and $\sin x \leq \cos x$, what is the range of x ?

49. the range of x ?

- A. $0 \leq x \leq \frac{\pi}{4}$
- B. $0 \leq x \leq \frac{\pi}{2}$
- C. $\frac{\pi}{4} \leq x \leq \frac{\pi}{2}$
- D. $\frac{\pi}{4} \leq x \leq \pi$
- E. $\frac{\pi}{2} \leq x \leq \pi$

82
50.

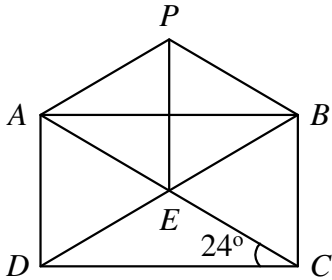


In the figure, $ABCD$ is a square of side $2a$. M and N are the mid-points of AB and CD respectively. h is the height of the parallelogram $MBND$. $h =$

- A. $\frac{1}{2}a$

- B. $\frac{2}{\sqrt{5}}a$
- C. $\frac{\sqrt{5}}{2}a$
- D. $\frac{2}{\sqrt{3}}a$
- E. $\frac{\sqrt{2}}{4}a$

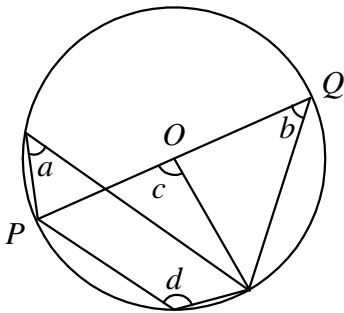
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51.



In the figure, $ABCD$ is a rectangle. AC and BD intersect at E . PAE is an equilateral triangle. $\angle PBC =$

- A. 48°
- B. 50°
- C. 52°
- D. 54°
- E. 60°

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52.

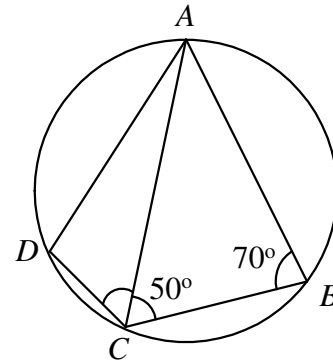


In the figure, O is the centre of the circle. PQ is a diameter. Which of the following is/are true?

- I. $a = b$
 - II. $c = 2a$
 - III. $c + d = 180^\circ$
- A. I only
 - B. I and II only

- C. I and III only
- D. II and III only
- E. I, II and III

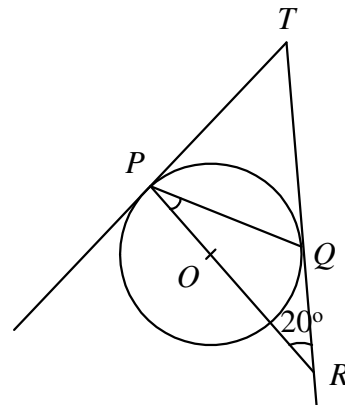
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53.



In the figure, the length of the minor arc CD is half the length of the minor arc BC . $\angle ACD =$

- A. 30°
- B. 35°
- C. 40°
- D. 45°
- E. 50°

82
54.



In the figure, TP and TQ touch the circle at P and Q respectively. R is the point on TQ produced such that PR passes through the centre O of the circle. $\angle QPR =$

- A. 55°
- B. 40°
- C. 35°
- D. 30°
- E. 20°

