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香港考試及評核局
HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY

2014年香港中學文憑考試
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION 2014

數學 **必修部分** **試卷一**
MATHEMATICS **COMPULSORY PART** **PAPER 1**

評卷參考
MARKING SCHEME

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Hong Kong Diploma of Secondary Education Examination
Mathematics Compulsory Part Paper 1

General Marking Instructions

1. It is very important that all markers should adhere as closely as possible to the marking scheme. In many cases, however, candidates will have obtained a correct answer by an alternative method not specified in the marking scheme. In general, a correct answer merits *all the marks* allocated to that part, unless a particular method has been specified in the question. Markers should be patient in marking alternative solutions not specified in the marking scheme.
2. In the marking scheme, marks are classified into the following three categories:

‘M’ marks	awarded for correct methods being used;
‘A’ marks	awarded for the accuracy of the answers;
Marks without ‘M’ or ‘A’	awarded for correctly completing a proof or arriving at an answer given in a question.

In a question consisting of several parts each depending on the previous parts, ‘M’ marks should be awarded to steps or methods correctly deduced from previous answers, even if these answers are erroneous. However, ‘A’ marks for the corresponding answers should NOT be awarded (unless otherwise specified).
3. For the convenience of markers, the marking scheme was written as detailed as possible. However, it is still likely that candidates would not present their solution in the same explicit manner, e.g. some steps would either be omitted or stated implicitly. In such cases, markers should exercise their discretion in marking candidates’ work. In general, marks for a certain step should be awarded if candidates’ solution indicated that the relevant concept/technique had been used.
4. In marking candidates’ work, the benefit of doubt should be given in the candidates’ favour.
5. In the marking scheme, ‘r.t.’ stands for ‘accepting answers which can be rounded off to’ and ‘f.t.’ stands for ‘follow through’. Steps which can be skipped are shaded whereas alternative answers are enclosed with rectangles. All fractional answers must be simplified.

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Solution	Marks	Remarks
<p>1. $\frac{(xy^{-2})^3}{y^4}$</p> <div style="background-color: #cccccc; padding: 2px; margin: 5px 0;"> $\frac{(x^3y^{-6})}{y^4}$ </div> <div style="background-color: #cccccc; padding: 2px; margin: 5px 0;"> $\frac{x^3y^{-10}}{y^4}$ </div> <p>$= \frac{x^3}{y^{10}}$</p>	<p>1M</p> <p>1M</p> <p>1A</p> <p>----- (3)</p>	<p>for $(ab)^m = a^m b^m$ or $(a^m)^n = a^{mn}$</p> <p>for $c^{-p} = \frac{1}{c^p}$ or $\frac{c^p}{c^q} = c^{p-q}$</p>
<p>2. (a) $a^2 - 2a - 3$ $= (a+1)(a-3)$</p> <p>(b) $ab^2 + b^2 + a^2 - 2a - 3$ <div style="background-color: #cccccc; padding: 2px; margin: 5px 0;"> $= ab^2 + b^2 + (a+1)(a-3)$ </div> $= b^2(a+1) + (a+1)(a-3)$ $= (a+1)(b^2 + a - 3)$</p>	<p>1A</p> <p>1M</p> <p>1A</p> <p>----- (3)</p>	<p>or equivalent</p> <p>for using the result of (a)</p> <p>or equivalent</p>
<p>3. (a) 200</p> <p>(b) 123</p> <p>(c) 123.4</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>----- (3)</p>	
<p>4. The median $= 1$</p> <p>The mode $= 2$</p> <p>The standard deviation <div style="background-color: #cccccc; padding: 2px; margin: 5px 0;"> ≈ 0.388819441 </div> ≈ 0.889</p>	<p>1A</p> <p>1A</p> <p>1A</p> <p>----- (3)</p>	<p>r.t. 0.889</p>

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Solution	Marks	Remarks
5. (a) $2(3m + n) = m + 7$ $6m + 2n = m + 7$ $n = \frac{7 - 5m}{2}$	1M 1A	for expanding or equivalent
$2(3m + n) = m + 7$ $3m + n = \frac{m + 7}{2}$ $n = \frac{7 - 5m}{2}$	1M 1A	for division or equivalent
(b) The decrease in the value of n $= 5$	1M 1M ----- (4)	
6. (a) The selling price of the toy $= 255(1 - 40\%)$ $= \$153$	1M 1A	
(b) Let $\$x$ be the cost of the toy. $(1 + 2\%)x = 153$ $x = 150$ Thus, the cost of the toy is $\$150$.	1M 1A ----- (4)	
7. (a) $f(2) = -33$ $4(2)^3 - 5(2)^2 - 18(2) + c = -33$ $c = -9$ $f(-1)$ $= 4(-1)^3 - 5(-1)^2 - 18(-1) - 9$ $= 0$ Thus, $x + 1$ is a factor of $f(x)$.	1M 1M 1A	f.t.
(b) $f(x) = 0$ $4x^3 - 5x^2 - 18x - 9 = 0$ $(x + 1)(4x^2 - 9x - 9) = 0$ $(x + 1)(x - 3)(4x + 3) = 0$ $x = -1$, $x = 3$ or $x = \frac{-3}{4}$ Note that -1 , 3 and $\frac{-3}{4}$ are rational numbers. Thus, the claim is agreed.	1M 1A ----- (5)	for $(x + 1)(px^2 + qx + r) = 0$ f.t.

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Solution	Marks	Remarks				
<p>8. (a) The coordinates of P' are $(5, 3)$. The coordinates of Q' are $(-19, -7)$.</p> <p>(b) The slope of PQ</p> $= \frac{5+7}{-3-2}$ $= \frac{-12}{5}$ <p>The slope of $P'Q'$</p> $= \frac{3+7}{5+19}$ $= \frac{5}{12}$ <p>So, the product of the slope of PQ and the slope of $P'Q'$ is -1 . Thus, PQ is perpendicular to $P'Q'$.</p>	<p>1A 1A</p> <p>1M 1A</p> <p>1</p> <p>----- (5)</p>	<p>either one</p> <p>either one</p>				
<p>9. (a) In $\triangle ABC$ and $\triangle BDC$,</p> <p style="margin-left: 40px;">$\angle BAC = \angle DBC$ (given)</p> <p style="margin-left: 40px;">$\angle ACB = \angle BCD$ (common \angle)</p> <p style="margin-left: 40px;">$\angle ABC = \angle BDC$ (\angle sum of \triangle)</p> <p style="margin-left: 40px;">$\triangle ABC \sim \triangle BDC$ (AAA)</p>		<p>[已知]</p> <p>[公共角]</p> <p>[\triangle内角和]</p> <p>(AA) (equiangular) [等角]</p>				
<p>Marking Scheme:</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="border: 1px solid black;">Case 1 Any correct proof with correct reasons.</td> <td style="border: 1px solid black; text-align: center;">2</td> </tr> <tr> <td style="border: 1px solid black;">Case 2 Any correct proof without reasons.</td> <td style="border: 1px solid black; text-align: center;">1</td> </tr> </table>			Case 1 Any correct proof with correct reasons.	2	Case 2 Any correct proof without reasons.	1
Case 1 Any correct proof with correct reasons.	2					
Case 2 Any correct proof without reasons.	1					
<p>(b) $\frac{CD}{BC} = \frac{BC}{AC}$</p> $\frac{CD}{20} = \frac{20}{25}$ $CD = 16 \text{ cm}$ <p>$BD^2 + CD^2$</p> $= 12^2 + 16^2$ $= 20^2$ $= BC^2$ <p>Thus, $\triangle BCD$ is a right-angled triangle.</p>	<p>1M</p> <p>1M</p> <p>1A</p> <p>----- (5)</p>	<p>f.t.</p>				

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Solution	Marks	Remarks
<p>10. (a) The distance of car A from town X at 8:15 in the morning</p> $= \frac{45}{120}(80)$ $= 30 \text{ km}$	<p>1M</p> <p>1A</p> <p>------(2)</p>	
<p>(b) Suppose that car A and car B first meet at the time t minutes after 7:30 in the morning.</p> $\frac{t}{120} = \frac{44}{80}$ $t = 66$ <p>Thus, car A and car B first meet at 8:36 in the morning.</p>	<p>1M</p> <p>1A</p> <p>------(2)</p>	
<p>(c) During the period 8:15 to 9:30 in the morning, car B travels 36 km while car A travels more than 36 km .</p> <p>So, the average speed of car A is higher than that of car B .</p> <p>Thus, the claim is disagreed.</p>	<p>1M</p> <p>1A</p>	<p>f.t.</p>
<p>The average speed of car A during the period 8:15 to 9:30 in the morning</p> $= \frac{80 - 30}{1.25}$ $= \frac{50}{1.25}$ $= 40 \text{ km/h}$ <p>The average speed of car B during the period 8:15 to 9:30 in the morning</p> $= \frac{80 - 44}{1.25}$ $= \frac{36}{1.25}$ $= 28.8 \text{ km/h}$ <p>Note that $40 > 28.8$.</p> <p>So, the average speed of car A is higher than that of car B .</p> <p>Thus, the claim is disagreed.</p>	<p>1M</p> <p>1A</p>	<p>accept $\frac{80}{2}$ -----</p> <p style="margin-left: 100px;">-----</p> <p style="margin-left: 100px;">either one</p> <p>-----</p> <p>f.t.</p> <p>------(2)</p>

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Solution	Marks	Remarks
<p>11. (a) The range $= 91 - 18$ $= 73$ thousand dollars</p> <p>The inter-quartile range $= 63 - 42$ $= 21$ thousand dollars</p>	<p>1M 1A</p>	<div style="border: 1px dashed black; padding: 5px; width: fit-content; margin: auto;"> <p>either one</p> </div>
<p>(b) The mean of the prices of the remaining paintings in the art gallery $= \frac{(33)(53) - 32 - 34 - 58 - 59}{33 - 4}$ $= \frac{1566}{29}$ $= 54$ thousand dollars</p> <p>Note that 32 and 34 are less than 55 . Also note that 58 and 59 are greater than 55 .</p> <p>The median of the prices of the remaining paintings in the art gallery $= 55$ thousand dollars</p>	<p>1M</p> <p>1A</p> <p>----- (3)</p>	
	1A	
	----- (3)	

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Solution	Marks	Remarks
<p>12. (a) The radius of C</p> $= \sqrt{(6-0)^2 + (11-3)^2}$ $= 10$ <p>Thus, the equation of C is $x^2 + (y-3)^2 = 10^2$.</p>	<p>1M</p> <p>1A</p> <p>----- (2)</p>	<p>$x^2 + y^2 - 6y - 91 = 0$</p>
<p>(b) (i) Let (x, y) be the coordinates of P.</p> $\sqrt{(x-0)^2 + (y-3)^2} = \sqrt{(x-6)^2 + (y-11)^2}$ $3x + 4y - 37 = 0$ <p>Thus, the equation of Γ is $3x + 4y - 37 = 0$.</p>	<p>1M</p> <p>1A</p>	
<div style="border: 1px solid black; padding: 5px;"> <p>The slope of AG</p> $= \frac{11-3}{6-0}$ $= \frac{4}{3}$ <p>Note that the slope of Γ is $\frac{-3}{4}$.</p> <p>Also note that the mid-point of AG is $(3, 7)$.</p> <p>The equation of Γ is</p> $y - 7 = \frac{-3}{4}(x - 3)$ $3x + 4y - 37 = 0$ </div>	<p>1M</p> <p>1A</p>	
<p>(ii) Γ is the perpendicular bisector of the line segment AG.</p>	<p>1A</p>	
<p>(iii) The perimeter of the quadrilateral $AQGR$</p> $= 4(10)$ $= 40$	<p>1M</p> <p>1A</p> <p>----- (5)</p>	

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Solution	Marks	Remarks
<p>13. (a) Let $f(x) = px^2 + q$, where p and q are non-zero constants. So, we have $4p + q = 59$ and $49p + q = -121$. Solving, we have $p = -4$ and $q = 75$. Therefore, we have $f(x) = 75 - 4x^2$. Thus, we have $f(6) = -69$.</p>	<p>1A 1M 1A 1A ----- (4)</p>	<p>for either substitution for both correct</p>
<p>(b) By (a), we have $a = -69$. Since $f(x) = 75 - 4x^2$, we have $f(-6) = f(6)$. So, we have $b = -69$.</p> <p style="margin-left: 20px;">AB $= 6 - (-6)$ $= 12$</p> <p style="margin-left: 20px;">The area of $\triangle ABC$ $= \frac{(12)(69)}{2}$ $= 414$</p>	<p>1M 1M 1A ----- (4)</p>	<p style="text-align: center;">} either one }</p> <p>can be absorbed</p>

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Solution	Marks	Remarks
<p>14. (a) The slant height of the circular cone</p> $= \sqrt{72^2 + 96^2}$ $= 120 \text{ cm}$ <p>The area of the wet curved surface of the vessel</p> $= \pi(72)(120) \frac{(96 - 60 + 28)^2 - (96 - 60)^2}{96^2}$ $= \pi(72)(120) \frac{64^2 - 36^2}{96^2}$ $= 2\,625\pi \text{ cm}^2$	<p>1M</p> <p>1M+1M</p> <p>1A</p>	
<p>Let R cm be the radius of the water surface.</p> <p>Then, we have $\frac{R}{72} = \frac{96 - 60 + 28}{96}$.</p> <p>Therefore, we have $\frac{R}{72} = \frac{64}{96}$.</p> <p>So, we have $R = 48$.</p> <p>Let r cm be the base radius of the lower part of the inverted right circular cone.</p> <p>Then, we have $\frac{r}{72} = \frac{96 - 60}{96}$.</p> <p>Therefore, we have $\frac{r}{72} = \frac{36}{96}$.</p> <p>So, we have $r = 27$.</p> <p>The area of the wet curved surface of the vessel</p> $= \pi(48)\sqrt{48^2 + 64^2} - \pi(27)\sqrt{27^2 + 36^2}$ $= \pi(48)(80) - \pi(27)(45)$ $= 2\,625\pi \text{ cm}^2$	<p>1M</p> <p>1M+1M</p> <p>1A</p>	<div style="border: 1px dashed black; width: 100px; height: 100px; margin: auto; display: flex; align-items: center; justify-content: center;"> either one </div>
	------(4)	
<p>(b) The volume of the circular cone</p> $= \frac{1}{3}\pi(72)^2(96)$ $= 165\,888\pi \text{ cm}^3$ <p>The volume of water in the vessel</p> $= 165\,888\pi \left(\frac{64^3 - 36^3}{96^3} \right)$ $= 40\,404\pi \text{ cm}^3$ $\approx 0.126932909 \text{ m}^3$ $> 0.1 \text{ m}^3$ <p>Thus, the claim is agreed.</p>	<p>1M</p> <p>1M+1A</p> <p>1A</p>	<p>f.t.</p>
<p>The volume of water in the vessel</p> $= \frac{1}{3}\pi(48)^2(64) - \frac{1}{3}\pi(27)^2(36)$ $= 49\,152\pi - 8\,748\pi$ $= 40\,404\pi \text{ cm}^3$ $\approx 0.126932909 \text{ m}^3$ $> 0.1 \text{ m}^3$ <p>Thus, the claim is agreed.</p>	<p>1M+1M+1A</p> <p>1A</p>	<p>f.t.</p>
	------(4)	

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Solution	Marks	Remarks
15. $\log_8 y - 0 = \frac{-1}{3}(\log_4 x - 3)$ $\log_8 y = \frac{-1}{3}\log_4 x + 1$ $\log_8 y = \log_4 x^{\frac{-1}{3}} + \log_4 4$ $\log_8 y = \log_4 4x^{\frac{-1}{3}}$ $\frac{\log_2 y}{\log_2 8} = \frac{\log_2 4x^{\frac{-1}{3}}}{\log_2 4}$ $\log_2 y = \frac{3}{2}\log_2 4x^{\frac{-1}{3}}$ $\log_2 y = \log_2 8x^{\frac{-1}{2}}$ $y = 8x^{\frac{-1}{2}}$	1M 1M 1A	
$\log_8 y - 0 = \frac{-1}{3}(\log_4 x - 3)$ $\log_8 y = \frac{-1}{3}\log_4 x + 1$ $\log_8 y = \log_4 x^{\frac{-1}{3}} + \log_4 4$ $\log_8 y = \log_4 4x^{\frac{-1}{3}}$ $y = 8^{\log_4 4x^{\frac{-1}{3}}}$ $y = 4^{\frac{3}{2}\log_4 4x^{\frac{-1}{3}}}$ $y = 4^{\log_4 8x^{\frac{-1}{2}}}$ $y = 8x^{\frac{-1}{2}}$	1M 1M 1A	
	------(3)	
16. Note that the numbers of dots in the patterns form an arithmetic sequence. The total number of dots in the first m patterns $= 3 + 5 + 7 + \dots + (2m + 1)$ $= \frac{m}{2}(3 + (2m + 1))$ $= m^2 + 2m$ $m^2 + 2m > 6888$ $m^2 + 2m - 6888 > 0$ $(m - 82)(m + 84) > 0$ $m < -84$ or $m > 82$ Thus, the least value of m is 83.	1M + 1A 1M 1A	accept $\frac{m}{2}((2)(3) + (m - 1)(2))$
	------(4)	

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Solution	Marks	Remarks
<p>17. (a) By sine formula, we have</p> $\frac{\sin \angle AVB}{AB} = \frac{\sin \angle VAB}{VB}$ $\frac{\sin \angle AVB}{18} = \frac{\sin 110^\circ}{30}$ $\angle AVB \approx 34.32008291^\circ$ $\angle VBA \approx 180^\circ - 110^\circ - 34.32008291^\circ$ $\angle VBA \approx 35.67991709^\circ$ $\angle VBA \approx 35.7^\circ$	1M	
	1A	r.t. 35.7°
	-----(2)	
<p>(b) By cosine formula, we have</p> $MP^2 = BP^2 + BM^2 - 2(BP)(BM) \cos \angle VBA$ $MP^2 \approx 9^2 + 15^2 - 2(9)(15) \cos 35.67991709^\circ$ $MP \approx 9.310329519 \text{ cm}$ $MN = \frac{BC}{2}$ $MN = 5 \text{ cm}$ <p>Note that $MP = NQ$.</p> <p>Let h cm be the height of the trapezium $PQNM$.</p> $h = \sqrt{MP^2 - \left(\frac{PQ - MN}{2}\right)^2}$ $h \approx \sqrt{9.310329519^2 - \left(\frac{10 - 5}{2}\right)^2}$ $h \approx 8.968402074$ <p>The area of the trapezium $PQNM$</p> $= \frac{h(MN + PQ)}{2}$ $\approx \frac{(8.968402074)(5 + 10)}{2}$ $\approx 67.26301555 \text{ cm}^2$ $< 70 \text{ cm}^2$ <p>Thus, the claim is agreed.</p>	1M	
	1A	f.t.

Solution	Marks	Remarks
<p>By cosine formula, we have</p> $MP^2 = BP^2 + BM^2 - 2(BP)(BM) \cos \angle VBA$ $MP^2 \approx 9^2 + 15^2 - 2(9)(15) \cos 35.67991709^\circ$ $MP \approx 9.310329519 \text{ cm}$ $MN = \frac{BC}{2}$ $MN = 5 \text{ cm}$ $\cos \angle MPQ = \frac{PQ - MN}{PM}$ $\cos \angle MPQ \approx \frac{10 - 5}{9.310329519}$ $\angle MPQ \approx 74.42384466^\circ$ <p>Note that $MP = NQ$.</p> <p>Let h cm be the height of the trapezium $PQNM$.</p> $\frac{h}{MP} = \sin \angle MPQ$ $\frac{h}{9.310329519} \approx \sin 74.42384466^\circ$ $h \approx 8.968402074$ <p>The area of the trapezium $PQNM$</p> $= h(MN) + \frac{1}{2}(MP)(BC - MN) \sin \angle MPQ$ $\approx (8.968402074)(5) + \frac{1}{2}(9.310329519)(10 - 5) \sin 74.42384466^\circ$ $\approx 67.26301555 \text{ cm}^2$ $< 70 \text{ cm}^2$ <p>Thus, the claim is agreed.</p>	<p>1M</p> <p>1M</p> <p>1M</p> <p>1M</p> <p>1A</p>	 <p>f.t.</p>
	----- (5)	

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Solution	Marks	Remarks
<p>18. (a) The slope of L_2</p> $= \frac{90-0}{45-180}$ $= \frac{-2}{3}$ <p>The equation of L_2 is</p> $y-90 = \frac{-2}{3}(x-45)$ $2x+3y-360=0$ <p>Thus, the system of inequalities is</p> $\begin{cases} 6x+7y \leq 900 \\ 2x+3y \leq 360 \\ x \geq 0 \\ y \geq 0 \end{cases}$	<p>1M</p> <p>1A</p> <p>1M+1A</p> <p>------(4)</p>	<p>or equivalent</p>
<p>(b) Let x and y be the numbers of wardrobes X and Y produced that month respectively.</p> <p>Now, the constraints are $6x+7y \leq 900$ and $2x+3y \leq 360$, where x and y are non-negative integers.</p> <p>Denote the total profit on the production of wardrobes by $\\$P$.</p> <p>Then, we have $P = 440x + 665y$.</p> <p>Note that the vertices of the shaded region in Figure 7 are the points $(0, 0)$, $(0, 120)$, $(45, 90)$ and $(150, 0)$.</p> <p>At the point $(0, 0)$, we have $P = (440)(0) + (665)(0) = 0$.</p> <p>At the point $(0, 120)$, we have $P = (440)(0) + (665)(120) = 79\,800$.</p> <p>At the point $(45, 90)$, we have $P = (440)(45) + (665)(90) = 79\,650$.</p> <p>At the point $(150, 0)$, we have $P = (440)(150) + (665)(0) = 66\,000$.</p> <p>So, the greatest possible profit is $\\$79\,800$.</p> <p>Thus, the claim is disagreed.</p>	<p>1A</p> <p>1M+1M</p> <p>1A</p>	<p>1M for testing a point + 1M for testing all points</p> <p>f.t.</p>
<p>Let x and y be the numbers of wardrobes X and Y produced that month respectively.</p> <p>Now, the constraints are $6x+7y \leq 900$ and $2x+3y \leq 360$, where x and y are non-negative integers.</p> <p>Denote the total profit on the production of wardrobes by $\\$P$.</p> <p>Then, we have $P = 440x + 665y$.</p> <p>Draw the straight line $88x + 133y = k$ on Figure 7, where k is a constant.</p> <p>It is found that P attains its greatest value at the point $(0, 120)$.</p> <p>So, the greatest value of P is $\\$79\,800$.</p> <p>Thus, the claim is disagreed.</p>	<p>1A</p> <p>1M+1M</p> <p>1A</p> <p>------(4)</p>	<p>$\left\{ \begin{array}{l} 1M \text{ for sliding straight line +} \\ 1M \text{ for straight line with negative slope} \end{array} \right.$</p> <p>f.t.</p>

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Solution	Marks	Remarks
<p>19. (a) The required probability</p> $= \frac{1}{6} + \left(\frac{5}{6}\right)\left(\frac{5}{6}\right)\left(\frac{1}{6}\right) + \left(\frac{5}{6}\right)\left(\frac{5}{6}\right)\left(\frac{5}{6}\right)\left(\frac{5}{6}\right)\left(\frac{1}{6}\right) + \dots$ $= \frac{1}{6} + \left(\frac{1}{6}\right)\left(\frac{25}{36}\right) + \left(\frac{1}{6}\right)\left(\frac{25}{36}\right)^2 + \dots$ $= \frac{\frac{1}{6}}{1 - \frac{25}{36}}$ $= \frac{6}{11}$	1M 1M 1A	r.t. 0.545
<p>Let p be the probability that Ada wins the first round of the game. Then, the probability that Billy wins the first round of the game is $\frac{5p}{6}$.</p> $p + \frac{5p}{6} = 1$ $\frac{11p}{6} = 1$ $p = \frac{6}{11}$ <p>Thus, the required probability is $\frac{6}{11}$.</p>	1M 1M 1A	r.t. 0.545
------(3)		
<p>(b) (i) Suppose that the player of the second round adopts Option 1.</p> <p>The probability of getting 10 tokens</p> $= (1)\left(\frac{1}{8}\right)$ $= \frac{1}{8}$ <p>The probability of getting 5 tokens</p> $= \frac{(7)(P_2^2)}{8^2}$ $= \frac{7}{32}$ <p>The expected number of tokens got</p> $= (10)\left(\frac{1}{8}\right) + (5)\left(\frac{7}{32}\right)$ $= \frac{75}{32}$	1M 1A 1M 1A	accept $\frac{8}{8^2}$ can be absorbed r.t. 2.34

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Solution	Marks	Remarks
<p>(ii) Suppose that the player of the second round adopts Option 2.</p> <p>The probability of getting 50 tokens</p> $= (1) \binom{1}{8} \binom{1}{8}$ $= \frac{1}{64}$ <p>The probability of getting 10 tokens</p> $= \frac{(6)(P_3^3)}{8^3}$ $= \frac{9}{128}$ <p>The probability of getting 5 tokens</p> $= (2) \binom{1}{8}^2 \binom{1}{8} + (6) \binom{1}{8} \binom{2}{8} + \binom{7}{32} \binom{2}{8}$ $= \frac{21}{256}$ <p>The expected number of tokens got</p> $= (50) \left(\frac{1}{64} \right) + (10) \left(\frac{9}{128} \right) + (5) \left(\frac{21}{256} \right)$ $= \frac{485}{256}$ <p>Note that $\frac{75}{32} > \frac{485}{256}$.</p> <p>Thus, the player of the second round should adopt Option 1.</p>	<p>1M</p> <p>1M</p> <p>1A</p>	<p>accept $\frac{(7)(2)(C_2^3)}{8^3}$</p> <p>f.t.</p>
<p>(iii) The probability of Ada getting no tokens</p> $= 1 - \binom{6}{11} \left(\frac{1}{8} + \frac{7}{32} \right)$ $= \frac{13}{16}$ $= 0.8125$ < 0.9 <p>Thus, the claim is incorrect.</p>	<p>1M + 1M</p> <p>1A</p>	<p>{ 1M for $1 - (a)p_1$ + 1M for $p_1 = p_2 + p_3$</p> <p>f.t.</p>
<p>The probability of Ada getting no tokens</p> $= \binom{6}{11} \left(1 - \frac{1}{8} - \frac{7}{32} \right) + \frac{5}{11}$ $= \frac{13}{16}$ $= 0.8125$ < 0.9 <p>Thus, the claim is incorrect.</p>	<p>1M + 1M</p> <p>1A</p>	<p>{ 1M for $(a)p_4 + 1 - (a)$ + 1M for $p_4 = 1 - p_5 - p_6$</p> <p>f.t.</p>
----- (10)		